Motion planning: sampling-based planners III basic modifications

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Known issues of sampling-based planning Mr security (MS) s

One may consider sampling-based planning as a "magic" tool
 ... but that's not true at all!

Sampling-based planners have many issues

- Narrow passage problem
 - Difficulty of sampling small region in C_{free} surrounded by C_{obs}
 - Problematic if (all) solutions have to pass that region
- Sensitivity to metric & parameters
 - How to measure distance in C?
 - Selecting a good metric is as difficult as motion planning!
 - Many methods have "too many" parameters
 - Some parameters are hidden (or not well described)
 - How to tune the parameters?
- Supporting functions
 - Collision detection & nearest-neighbor search
 - Fast and reliable implementation

How do we recognize the issue? \rightarrow performance measurement!

Narrow passage problem

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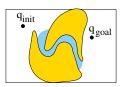


Narrow passage (NP)

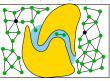
- A region $\mathcal{R} \subseteq \mathcal{C}_{\text{free}}$ with a small volume $vol(\mathcal{R}) < vol(\mathcal{C})$
- Probability that a random sample falls to $\mathcal R$ is $\sim \textit{vol}(\mathcal R)/\textit{vol}(\mathcal C)$
- NP are problematic if their removal changes connectivity of $\mathcal{C}_{\text{free}}$
- NP are regions in $\mathcal{C} \to \text{they}$ are given implicitly
- Location/size/volume/shape of NPs is not known!

Consequences of having NP

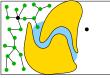
- ullet PRM builds unconnected roadmaps o no solution
- RRT/EST cannot enter NP \rightarrow no solution
- Number of samples must be significantly increased
- Runtime is increased



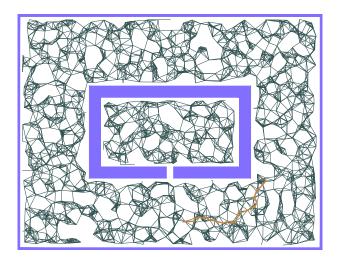
narrow passage (NP)



PRM & NP

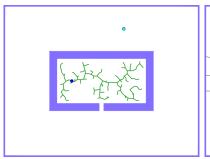


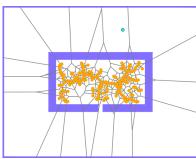
RRT/EST & NP



Narrow passage & RRT









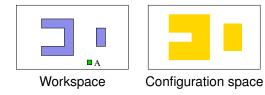


- Narrow passages are in C
- Sometimes, we cannot (easily) see/estimate them from workspace!
- What makes the narrow passage in the Alpha-puzzle benchmark?

How does C_{obs} appears?



- Can we guess shape of Cobs based on workspace?
- $vol(A) \ll vol(O)$



vol(A) < vol(O)



• When obstacles ${\cal O}$ dominate, they mostly influence the shape of ${\cal C}_{\rm obs}$

How does \mathcal{C}_{obs} appear?

- Let $X, Y \subset \mathbb{R}^n$, X and Y are nonempty
- Brunn-Minkowski theorem:

$$\operatorname{vol}(X \oplus Y) \geq \left(\operatorname{vol}(X)^{\frac{1}{n}} + \operatorname{vol}(Y)^{\frac{1}{n}}\right)^n$$

- $vol(\mathcal{C}_{obs})$ is larger than $min(vol(\mathcal{A}), vol(\mathcal{O}))$
- vol(C_{obs}) can be much larger!

Example: vol(A) = vol(O)





Configuration space

Improvements



Why improvements of PRM/RRT/EST?

 To cope with the narrow passage problem, improve path quality, speed-up planning, to enable planning in specific cases

Main tricks

- Change distribution of random samples
- Dedicated metrics
- Improved nearest-neighbor search
- Use suitable local planners
- Improve collision-detection

```
initialize tree \mathcal{T} with q_{\text{init}}
for i=1,\ldots,I_{max} do

|q_{\text{rand}}| = \text{generate randomly in } \mathcal{C}
|q_{\text{near}}| = \text{find nearest node in } \mathcal{T} \text{ towards}
|q_{\text{rand}}| = \text{localPlanner from } q_{\text{near}} \text{ towards}
|q_{\text{rand}}| = \text{if } canConnect(q_{\text{near}}, q_{\text{new}}) \text{ then}
|\mathcal{T}. \text{addNode}(q_{\text{new}})| = \text{if } \varrho(q_{\text{new}}, q_{\text{goal}}) < d_{goal} \text{ then}
|\mathcal{T}. \text{return path from } q_{\text{init}} \text{ to } q_{\text{new}}
```

Improvements



- Many existing modifications of sampling-based planners, look at surveys
- Next slides present the basic principle of improvements
- ◆Elbanhawi, M., & Simic, M. (2014). Sampling-based robot motion planning: A review. IEEE access, 2, 56-77.
- ◆Veras, Luiz Gustavo D. O., Felipe L. L. Medeiros, and Lamartine N. F. Guimaraes. Systematic Literature Review of Sampling Process in Rapidly-Exploring Random Trees. IEEE Access 7 (2019)

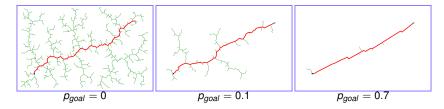
RRT improvement I: goal bias

Observation

- RRT tree grows towards random samples
- If we samples some region more dense, the tree is "attracted" to grow there

Goal-bias

- Random sample q_{rand} is generated in \mathcal{C} with probability $(1 p_{\text{goal}})$, otherwise it is set to $q_{\text{rand}} = q_{\text{goal}}$
- The rest of RRT algorithm is the same
- Improves the performance if the tree can directly reach the goal
- Decreases the performance if the tree is hindered by obstacles



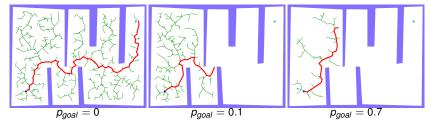
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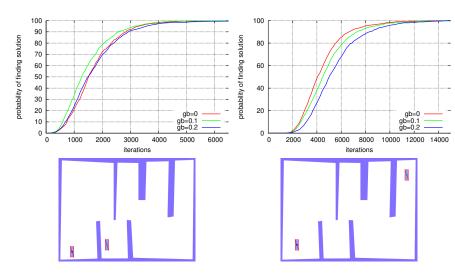
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RRT improvement I: goal bias



Goal-bias may improve or even worse the performance!



RRT improvement II: guided sampling





Observation

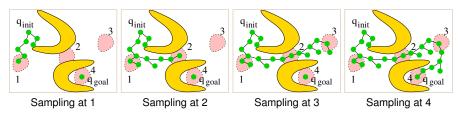
- Goal-bias attracts the tree towards $q_{\rm goal}$, but the tree may be blocked by obstacles
- Generalization: we can attract the tree toward any region $\mathcal{R} \subseteq \mathcal{C}$ if we sample \mathcal{R} densely

RRT + goal-bias

Guiding path

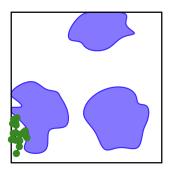
Guided-based sampling

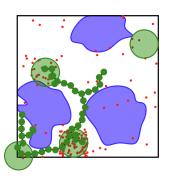
- Estimate a path that can "guide" the tree in the C-space
- Generate q_{rand} around the path-waypoints (starting from first waypoint) until the tree reaches the waypoint
- Then generate q_{rand} around the next waypoint



Guided sampling







Guided sampling







How to compute the guiding path?

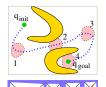
- Generally, the guiding path has to be located in \mathcal{C} !!
- Finding a good guiding path has the same complexity as the original planning problem!
- (i.e., guiding sampling is 'planning solved by planning')
- Practically, we have two options

Guiding path in W

- Path is computed in workspace geometric planning (Voronoi diagram, Visibility graph, etc.)
- Suitable for low-dimensional problems
- The remaining dimensions are sampled uniformly

Guiding path in C

Path is computed in C by a simplified search





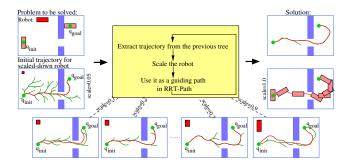
 $q = (x, y, \varphi)$ (x, y) from the path φ randomly

Computing guiding path in C



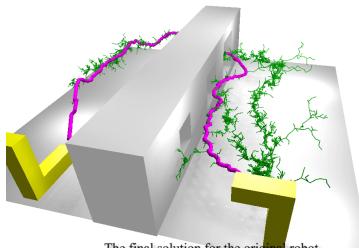
Guiding path in C

- Problem is simplified relaxation of constraints
- For example, robot is scaled-down
- Solve simplified planning problem
- Use the solution to generate random samples along it
- The process can be iterative



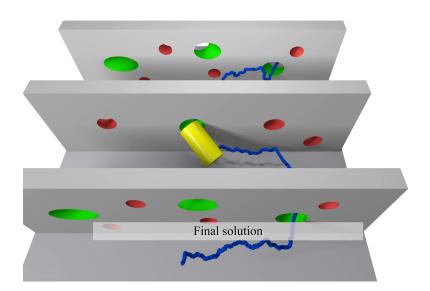
Computing guiding path in $\mathcal C$





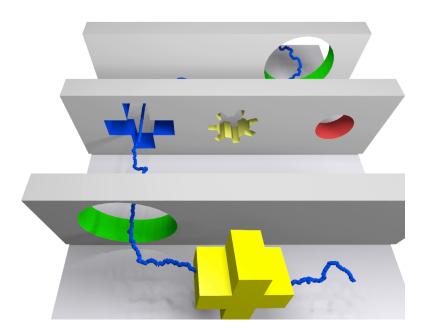
The final solution for the original robot

Computing guiding path in $\ensuremath{\mathcal{C}}$



Computing guiding path in $\ensuremath{\mathcal{C}}$



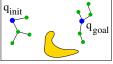


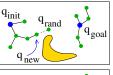
RRT improvement III: bidirectional search

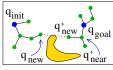
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- Use two trees: \mathcal{T}_i rooted at $q_{ ext{init}}, \, \mathcal{T}_g$ rooted $q_{ ext{goal}}$
- One tree expands towards q_{rand}, second tree expands towards q_{new} of the first tree

```
\mathcal{T}_i.addNode(q_{init})
    \mathcal{T}_q.addNode(q_{goal})
     for i = 1, ..., I_{max} do
             q_{\rm rand} = generate randomly in C
             q_{\text{near}} = find nearest node in T_i towards q_{\text{rand}}
             q_{\text{new}} = \text{localPlanner from } q_{\text{near}} \text{ towards } q_{\text{rand}}
             if canConnect(q_{near}, q_{new}) then
 7
                     \mathcal{T}_i.addNode(q_{new})
                     \mathcal{T}_i.addEdge(q_{\text{near}}, q_{\text{new}})
                     q'_{\text{near}} = find nearest node in \mathcal{T}_g towards q_{\text{new}}
10
                     q'_{\text{new}} = localPlanner from q_{\text{near}} towards q_{\text{rand}}
11
                     if canConnect(q'_{near}, q'_{new}) then
12
                            \mathcal{T}_a.addNode(q_{new})
13
                            \mathcal{T}_a.addEdge(q_{\text{near}}, q_{\text{new}})
14
                            if canConnect(q'_{new}, q_{new}) then
15
                                    joint trees
16
                                    return path from q_{init} to q_{goal}
17
             \mathcal{T}_i, \mathcal{T}_a = \mathcal{T}_a, \mathcal{T}_i
18
                                                                                   // swap trees
```

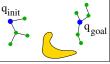


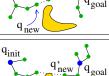


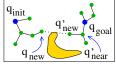


RRT improvement III: bidirectional search

- Use two trees: \mathcal{T}_i rooted at q_{init} , \mathcal{T}_q rooted q_{goal}
- One tree expands towards q_{rand} , second tree expands towards q_{new} of the first tree
- Helps to enter narrow passages (sometimes)
- Connection of two trees
 - Computationally intensive
 - To speed up, performs only if $\varrho(q_{\text{new}}, q'_{\text{new}})$ is small enough
 - Difficult if motion model/constraints have to be considered
- Balanced trees: swap trees if $|\mathcal{T}_i| > |\mathcal{T}_a|$







PRM variants I: sampling strategies

Original PRM/sPRM

- Uniform sampling q ∼ U(C)
- Gaussian sampling: two-samples
 - Uniform sample $q_1 \sim U(C)$, then another sample $q_2 \sim N(q, \Sigma)$ (around q_1 from Gaussian distribution)
 - Ignore if $q_1,q_2\in\mathcal{C}_{\text{free}}$ or $q_1,q_2\in\mathcal{C}_{\text{obs}}$, otherwise
 - add the collision-free one to the roadmap
 - Generates the random samples near \mathcal{C}_{obs} only!

Gaussian + uniform

- Combination of two previous methods
- More dense sampling around \mathcal{C}_{obs} than basic PRM

Bridge test

- Generate q_1 and q_2 using the Gaussian method
- Determine the midpoint q' on the line segment $|q_1,q_2|$
- Use q' if $q' \in \mathcal{C}_{\text{free}}$ and $q_1, q_2 \in \mathcal{C}_{\text{obs}}$



Uniform



Gaussian



Gaussian + Uniform

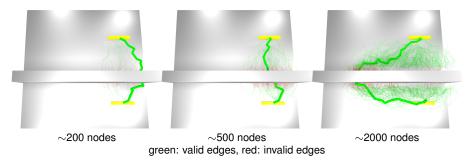


Bridge-Test

PRM variants II: Lazy PRM



- Build PRM roadmap, but without collision detection of edges
- After a path is found, edges are checked for collision and the path is recalculated
- If no path is found, extend the roadmap by new samples/edges
- Otherwise, the path is collision-free



- Faster planning in certain scenarios, but not always!
- R. Bohlin and L. E. Kavraki, "Path planning using lazy PRM," IEEE ICRA, 2000.

