## Maximum augmenting sequence of spanning trees

Let $G$ be an unempty simple undirected connected weighted graph, $G=(\mathrm{V}, \mathrm{E}, w)$, $w: \mathrm{E} \rightarrow\{0,1,2,3, \ldots\}$. In this problem, we suppose that the weights of all edges of $G$ are mutually different.

At first, we describe the problem less formally. Let $T_{1}$ be a spanning tree of $G$. The central part of the problem is to create another spanning tree of $G$, say $T_{2}$, which differs a little from $T_{1}$ and which we will call an augment of $\boldsymbol{T}_{1}$. The process of creating $T_{2}$ consists of the following:

1. Find a cheap edge $e_{1}$ in $T_{1}$.
2. Find an expensive edge $e_{2}$, which belongs to $G$ but not to $T_{1}$.
3. Remove the cheap edge $e_{1}$ from $T_{1}$ and insert the expensive edge $e_{2}$ into $T_{1}$.

Steps 1.- 3. must be completed in such way that the resulting subgraph, now called $T_{2}$, will again be a spanning tree of $G$. Also, the weight of $T_{2}$ must be bigger than the weight of $T_{1}$ and maximum possible. As there can be more pairs of edges ( $e_{1}, e_{2}$ ) which satisfy these conditions, we additionally demand that the weight $w\left(e_{1}\right)$ must also be maximum possible among those pairs of edges.


Image 1a. Graph $G$ and its spanning trees $T_{1}$ and $T_{2}$. $T_{2}$ is an augment of $T_{1}$.


Image 1b. $T_{2}$ is not an augment of $T_{1}$.


Image 1c. $T_{2}$ is not an augment of $T_{1}$.

Example. In the image above there is a highlighted spanning tree $T_{1}$ of the graph $G$. To create a spanning tree $T_{2}$ (also highlighted) which is an augment of $T_{1}$ we chose the pair of edges ( $\{\mathrm{C}, \mathrm{E}\},\{\mathrm{D}, \mathrm{G}\}$ ). The weight of $T_{2}$ is then 45. This can be seen in the image 1a. We cannot choose, for example, the pair ( $\{C, D\},\{B, D\}$ ) because the weight of $T_{2}$ would be only 38 as can be seen in the image 1 b . Also, as illustrated in the image 1 c , we cannot choose the pair ( $\{A, C\},\{B, D\}$ ) because although the weight of $T_{2}$ would be 45 , which is maximum possible, the weight of the edge $\{A, C\}$ is less than the weight of the first edge of the pair $(\{C, E\},\{D, G\})$ used in the image 1a.

For the sake of completeness we provide also a formal definition of the augment tree. You may skip this section if the informal description is sufficient for you.
Let $T$ be a spanning tree of $G$. We say that an ordered pair of edges $\left(e_{1}, e_{2}\right) \in \mathrm{E} \times \mathrm{E}$ is a $\boldsymbol{T}$-augmenting pair of edges if both following conditions hold:

1. $e_{1} \in \mathrm{E}(T), e_{2} \in \mathrm{E}(G)-\mathrm{E}(T)$.
2. The difference $w\left(e_{2}\right)-w\left(e_{1}\right)$ is positive and maximum possible.

We say that a $T$-augmenting pair of edges $\left(e_{1}, e_{2}\right)$ is a proper $T$-augmenting pair if the value of $w\left(e_{1}\right)$ is maximum among all $T$-augmenting pairs of edges.
Let $T_{1}$ and $T_{2}$ be two spanning trees of a $G$. We say that $T_{2}$ is an augment of $\boldsymbol{T}_{\mathbf{1}}$ if there is a proper $T_{1}$-augmenting pair $\left(e_{1}, e_{2}\right)$ such that $\mathrm{E}\left(T_{2}\right)=\left\{\mathrm{E}\left(T_{1}\right)-e_{1}\right\} \cup e_{2}$.

We say that a sequence $\left(T_{1}, T_{2}, \ldots, T_{D}\right),(D>0)$ of spanning trees of $G$ is a maximum augmenting sequence of $\boldsymbol{G}$ when both following conditions hold:

1. $T_{1}$ is a minimum spanning tree of $G$.
2. $T_{k}$ is a augment of $T_{k-1}$, for $k=2,3, \ldots, D$.

Note that for some values of $D$ the maximum augmenting sequence might be undefined.

## The task

We have to find the weight of the last element of the maximum augmenting sequence of the given graph $G$. We consider the weight of a graph to be the sum of weights of all its edges.

## Input

The first line of input contains three positive integers $N, M, D$ separated by space. The integers represent the number of vertices, the number of edges and the value $D$ specified above. Next, there are $M$ lines, each specifies one edge by three integers $a, b, c$ separated by space. The integers $a$ and $b$ represent the edge $\{a, b\}$ and $c$ represent its weight. We suppose that the vertices of the graph are labeled $0,1, \ldots N-1$. Input values satisfy $D \leq N \leq 2000$.

## Output

The output consists of a single line containing the weight of the last element of the maximum augmenting sequence $\left(T_{1}, T_{2}, \ldots, T_{D}\right)$ of the input graph. The sequence is always defined.

Example 1
Input
10133
016
1210
234
345
569
671
788
893
0513
167
272
3811
4912


Output
64
Image 2. The picture shows the maximum augmenting sequence $\left(T_{1}, T_{2}, T_{3}\right)$ of the input graph in Example 1. The edges of the spanning trees are highlighted.
Example 2

## Input

7217
200
323
425
507
649
4111
3013
4315
3117
5119
1021
2123
4025
6527
5429
6331
5233
5335
6237
6139
6041

